

Probability Cheatsheet

A quick reference guide to probability concepts, formulas, and distributions, covering basic probability, conditional probability, random variables, and common distributions.



Basic Probability Concepts

| Definitions | | Basic Probability Formula | Probability Rules | | |
|----------------------|---|--|---|--|--|
| Probability: | A measure of the likelihood that an event will occur. It is quantified as a number between O and 1, where O indicates impossibility and 1 indicates | The probability of an event <i>E</i> occurring is defined as: P(E) = \text{Number of favorable outcomes}}{Total number of possible outcomes}} = \frac{n(E)}{n(S)} Where: • P(E) is the probability of event <i>E</i> . • n(E) is the number of outcomes in event <i>E</i> . • n(S) is the number of outcomes in the sample space <i>S</i> . | Rule 1: Probability Range | The probability of any event <i>E</i> must be between 0 and 1: 0 \le P(E) \le 1 | |
| | certainty. | | Rule 2: Probability of Sample Space | The probability of the entire sample space <i>S</i> is 1: | |
| Experiment: | A process or action that has observable outcomes. | | | | |
| Sample Space | The set of all possible outcomes | | | P(S) = 1 | |
| (5): | or an experiment. | | Rule 3: Complement Rule | The probability of an | |
| Event (E): | A subset of the sample space, representing a specific outcome or set of outcomes. | | | event <i>E</i> not occurring is: | |
| Outcome: | come: A possible result of an | | | P(E') = 1 - P(E) | |
| experiment. | | Rule 4: Addition Rule | For any two events A | | |
| Mutually | Events that cannot occur at the | s that cannot occur at the | | and B: | |
| Exclusive Events: | same time (i.e., they have no outcomes in common). | | | P(A \cup B) = P(A) + P(B) - P(A \cap B) | |
| | | | Rule 5: Addition Rule for Mutually Exclusive Events | If A and B are mutually exclusive: | |

Conditional Probability and Independence

Conditional Probability

Independence of Events

| Soliditional Probability | independence of Events | | bayes medicin | |
|--|---------------------------|---|--|--|
| Conditional probability is the probability of an event A occurring given that another event B has already occurred. It is denoted as $P(A B)$ and calculated as: | Definition | Two events A and B are independent if the occurrence of one does not affect the probability of the other. | Bayes' Theorem describes the probability of an event based on prior knowledge of conditions related to the event. It is given by: P(A B) = \frac{P(B A) \cdot P(A)}{P(B)} | |
| $P(A B) = \{frac\{P(A \setminus cap B)\}\{P(B)\}, where P(B) > 0$ | Independence Condition | Events A and B are independent if and only if: P(A \cap B) = P(A) \cdot | Where: P(A B) is the posterior probability of A give B. P(B A) is the likelihood of B given A. | |

| | P(A \cap B) = P(A) \cdot P(B) | |
|--------------------------------|------------------------------------|---|
| Conditional Probability and | If A and B are independent, then: | |
| independence | P(A B) = P(A) and P(B A) = P(B) | 1 |

Bayes' Theorem

| vent based on phor knowledge of conditions | |
|--|--|
| elated to the event. It is given by: | |
| (A B) = \frac{P(B A) \cdot P(A)}{P(B)} | |
| /here: | |
| P(A B) is the posterior probability of A given | |

 $P(A \setminus cup B) = P(A) +$

P(B)

А.

- P(A) is the prior probability of A. •
- P(B) is the prior probability of B.

In terms of sample space:

 $P(A|B) = \frac{P(B|A) \det P(A)}{P(B|A) \det P(A)}$ $P(A) + P(B|A') \setminus cdot P(A')$

Random Variables and Distributions

| Random Variables | | Probability Density Function (PDF) | Expected Value (Mean) | |
|--|--|--|--|--|
| Definition: Discrete Random Variable: Continuous | A random variable is a variable whose value is a numerical outcome of a random phenomenon. A variable whose value can only take on a finite number of values or a countably infinite number of values. A variable whose value can take | For a continuous random variable X, the probability density function (PDF) gives the relative likelihood that X will take on a specific value. The probability that X falls within a certain interval [a, b] is given by the integral of the PDF over that interval: $P(a \leq b) = \\int_{a}^{b} f(x) dx$ Where f(x) is the PDF. | The expected value (or mean) of a random variable X is the weighted average of its possible values: For discrete random variable: E(X) = \sum x \cdot P(X = x) For continuous random variable: E(X) = \int x \cdot f(x) dx | |
| Random Variable: | on any value within a given range. | Cumulative Distribution Function (CDF) | Variance: | The variance measures the spread |
| Probability Mass Function (PMF) For a discrete random variable X, the probability mass function (PMF) gives the probability that X takes on a specific value x: P(X = x) | | The cumulative distribution function (CDF) gives the probability that a random variable X takes on a value less than or equal to x: $F(x) = P(X \mid x)$ | | of the distribution of a random variable around its mean: Var(X) = E[(X - E(X))^2] Alternative formula: Var(X) = E[X^2] - (E[X])^2 |
| | | | Standard Deviation: | The standard deviation is the square root of the variance and provides a measure of the typical deviation of values from the mean: SD(X) = \sqrt{Var(X)} |

Discrete Distributions

| Discrete Distributions | Continuous Distributions |
|---|---|
| Bernoulli Distribution Represents the probability of success or failure of a single binary event. PMF: P(X = x) = p^x (1-p)^{(1-x)}, where x \in {0, 1} and p is the | Uniform Distribution Represents a constant probability over a given interval. PDF: f(x) = \frac{1}{b-a} for a \le x \le b, where a and b are the interval |
| probability of success. E(X) = p Var(X) = p(1-p) | endpoints. • E(X) = \frac{a+b}{2} • Var(X) = \frac{(b-a)^2}{12} |
| Binomial Distribution | Exponential Distribution |
| Represents the number of successes in a fixed number of independent Bernoulli trials. PMF: P(X = k) = \binom{n}{k} p^k (1-p)^{(n-k)}, where n is the number of trials, k is the number of successes, and p is the probability of success in a single trial. E(X) = np Var(X) = np(1-p) | Represents the time until an event occurs in a Poisson process. PDF: f(x) = \lambda e^{-\lambda x} for x \ge 0, where \lambda is the rate parameter. E(X) = \frac{1}{\lambda} Var(X) = \frac{1}{\lambda^2} |
| Poisson Distribution Represents the number of events occurring in a fixed interval of time or space. PMF: P(X = k) = \frac{\lambda^k e^{-\lambda}}{k!}, where \lambda is the average rate of events. E(X) = \lambda Var(X) = \lambda | Represents a symmetric, bell-shaped distribution characterized by its mean and standard deviation. PDF: f(x) = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}, where \mu is the mean and \sigma is the standard deviation. E(X) = \mu Var(X) = \sigma^2 |